$$i\sum_{\nu} S_{\mu\nu} \frac{\partial c_{\nu n}}{\partial t} = \sum_{\nu} (H_{\mu\nu} + P_{\mu\nu}) c_{\nu n} + i\sum_{\nu} \mathbf{G}_{\mu\nu} \cdot \mathbf{v}^{\nu} c_{\nu n}$$
 (1)

 $\quad \text{where} \quad$

$$\mathbf{G}_{\mu\nu} = \langle \Phi_{\mu} | \hat{S} | \boldsymbol{\nabla} \Phi_{\nu} \rangle \tag{2}$$

and \mathbf{v}^{ν} is the velocity of the atom hosting basis function $\nu.$